



# ST. LAWRENCE HIGH SCHOOL

A JESUIT CHRISTIAN MINORITY INSTITUTION



Sub: Algebra and Geometry

Class: 7

Date: 08.05.20

## STUDY MATERIAL: ALGEBRAIC EXPRESSIONS

### Concepts, Explanations and Solved Numerical Problems

Introduction to Algebraic Expressions

Constant

**Constant** is a quantity which has a fixed value.

Definition of Variables

- Any algebraic expression can have any number of variables and constants.
  - Variable
    - A variable is a quantity that is prone to change with the context of the situation.
    - $a, x, p, \dots$  are used to denote variables.
  - Constant
    - It is a quantity which has a fixed value.
    - In the expression  $5x+4$ , the variable here is  $x$  and the constant is 4.
    - The value  $5x$  and 4 are also called terms of expression.
    - In the term  $5x$ , 5 is called the coefficient of  $x$ . Coefficients are any numerical factor of a term.

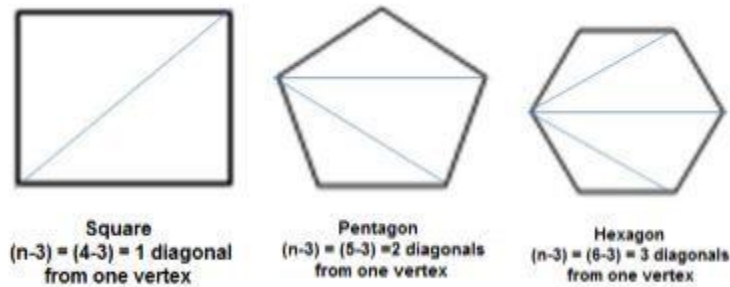
### Algebra as Patterns

Writing Number patterns and rules related to them

- If a natural number is denoted by  $n$ , its successor is  $(n + 1)$ .  
Example: Successor of  $n=10$  is  $n+1 = 11$ .
- If a natural number is denoted by  $n$ ,  $2n$  is an even number and  $(2n+1)$  an odd number.  
Example: If  $n=10$ , then  $2n = 20$  is an even number and  $2n+1 = 21$  is an odd number.

Writing Patterns in Geometry

- Algebraic expressions are used in writing patterns followed by geometrical figures.  
Example: Number of diagonals we can draw from one vertex of a polygon of  $n$  sides is  $(n - 3)$ .



### Algebraic Expressions:

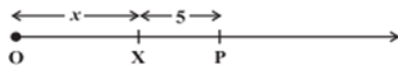
Any expression containing constants, variables, and the operations like addition, subtraction, etc. is called as an algebraic expression.

**Example:**  $5x$ ,  $2x - 3$ ,  $x^2 + 1$ , etc.

### Relation between number line and expression:

For any given expression of the form  $(a + b)$ , where  $a$  is variable and  $b$  is constant then the value of this expression will always lie at  $b$  units after the point  $a$  on the number line.

**Example 1:** The following figure shows a number line drawn for the expression  $x + 5$ .



Here,  $X$  represents the variable  $x$  which is unknown.

Thus, the final point will definitely be at 5 units from  $X$  which is denoted by  $P$ .

### Formation of Algebraic Expressions

- Variables and numbers are used to construct terms.
- These terms along with a combination of operators constitute an algebraic expression.
- The algebraic expression has a value that depends on the values of the variables.
- For example, let  $6p^2 - 3p + 5$  be an algebraic expression with variable  $p$   
 The value of the expression when  $p=2$  is,  
 $6(2)^2 - 3(2) + 5 \rightarrow 6(4) - 6 + 5 = 23$   
 The value of the expression when  $p=1$  is,  
 $6(1)^2 - 3(1) + 5 \rightarrow 6 - 3 + 5 = 8$

#### 1. Term:

A term is either a single number or variable and it can be combination of numbers and variable. They are usually separated by different operators like  $+$ ,  $-$ , etc.

**Example 1:** Some example of terms are  $y$ ,  $5$ ,  $2x$ , etc.

**Example 2:** Consider an expression  $6x - 7 = 2$ .  
Then, the terms in this expression are  $6x$ ,  $-7$  and  $2$ .

**Example 3:** Identify the terms for  $0.7a - 1.2b + 0.5ab$ .  
**Solution:** The terms for given expression are  $0.7a$ ,  $-1.2b$  and  $0.5ab$ .

## 2. Factors:

Factors can be product of numbers or number and variable.

*Example 1:* Term  $7x$  is made of two factors 7 and  $x$ .

*Example 2:* Number 6 is made of two factors 2 and 3, 1 and 6.

## 3. Coefficient

The number multiplied to variable is called as coefficient.

*Example 1:* The coefficient of the term  $2x$  will be 2.

*Example 2:* The coefficient of the term  $5ab$  will be 5.

*Example 3:* Identify the coefficients for  $0.7a - 1.2b + 0.5ab$ .

*Solution:* The coefficients for the given expression are 0.7, -1.2 and 0.5.

## Degree of a Polynomial (with one variable)

A polynomial looks like this:

The **Degree** (for a polynomial with one variable, like  $x$ ) is:

the **largest exponent** of that variable.

More Examples:

$4x$	The Degree is <b>1</b> (a variable without an exponent actually has an exponent of 1)
$4x^3 - x + 3$	The Degree is <b>3</b> (largest exponent of $x$ )
$x^2 + 2x^5 - x$	The Degree is <b>5</b> (largest exponent of $x$ )
$z^2 - z + 3$	The Degree is <b>2</b> (largest exponent of $z$ )

## Names of Degrees

When we know the degree we can also give it a name!

Degree	Name	Example
0	Constant	7
1	Linear	$x+3$

2	Quadratic	$x^2-x+2$
3	Cubic	$x^3-x^2+5$
4	Quartic	$6x^4-x^3+x-2$
5	Quintic	$x^5-3x^3+x^2+8$

Example:  $y = 2x + 7$  has a degree of 1, so it is a **linear** equation

Example:  $5w^2 - 3$  has a degree of 2, so it is **quadratic**

Higher order equations are **usually** harder to solve:

- Linear equations are **easy** to solve
- Quadratic equations are **a little harder** to solve
- Cubic equations are harder again, but **there are formulas** to help
- Quartic equations can also be solved, but the formulas are **very complicated**
- Quintic equations have no formulas, and **can sometimes be unsolvable!**

### Degree of a Polynomial with More Than One Variable

When a polynomial has more than one variable, we need to look at **each term**. Terms are separated by + or - signs.

For **each term**:

- Find the degree by **adding the exponents of each variable** in it,

The **largest** such degree is the degree of the polynomial.

Example: what is the degree of this polynomial:

Checking each term:

- $5xy^2$  has a degree of **3** (x has an exponent of 1, y has 2, and  $1+2=3$ )
- $3x$  has a degree of **1** (x has an exponent of 1)
- $5y^3$  has a degree of **3** (y has an exponent of 3)
- **3** has a degree of 0 (no variable)

The largest degree of those is 3 (in fact two terms have a degree of 3), so the polynomial has a degree of **3**

Example: what is the degree of this polynomial:

$$4z^3 + 5y^2z^2 + 2yz$$

Checking each term:

- $4z^3$  has a degree of **3** (z has an exponent of 3)
- $5y^2z^2$  has a degree of **4** (y has an exponent of 2, z has 2, and  $2+2=4$ )
- $2yz$  has a degree of **2** (y has an exponent of 1, z has 1, and  $1+1=2$ )

The largest degree of those is 4, so the polynomial has a degree of 4

### Writing it Down

Instead of saying "*the degree of (whatever) is 3*" we write it like this:

$$\text{deg}(5xy^2 - 3x) = 3$$

### 4. Monomials:

The expressions which have only one term are called as monomials.

*Example:* 10, 3x, 5xy, 2x<sup>2</sup>, etc. are some monomials.

### 5. Binomials:

The expressions which have two terms are called as binomials.

*Example:* x + 10, 3x + 1, a + b, 7x<sup>2</sup> + y<sup>2</sup> etc. are some binomials.

### 6. Trinomials:

The expressions which have three terms are called as trinomials.

*Example:* 2x + y + 10, 3y + 3x, a + b + c, 7x<sup>2</sup> + y<sup>2</sup> + 7 etc. are some trinomials.

### 7. Polynomials:

The expression which contains one or more terms with non-zero coefficient is called a polynomial. A polynomial can have any number of terms.

*Example 1:* 10, a + b, 7x + y + 5, w + x + y + z, etc.

*Example 2:* Classify following polynomials into monomials, binomials, trinomials or others:

(a) a + b      (b) 7      (c) ab + bc + cd + da      (d) 5x - 5y + 13xy

*Solution:* (a) Binomial      (b) Monomial      (c) Polynomial      (d) Trinomial

### 8. Like terms:

The terms which have same variables are known as like terms.

*Example:* 5x and 7x; 2xy and 3yx; 4x<sup>2</sup>, 7x<sup>2</sup>, 9x<sup>2</sup> and x<sup>2</sup>; etc. are some like terms.

### 9. Unlike terms:

The terms which do not have the same variables are known as unlike terms.

*Example:* 5x and 7y; 2xy and 3ax; 4x<sup>2</sup>, 7y<sup>2</sup> and 9z<sup>2</sup>; etc. are some unlike terms.

### Addition and Subtraction of Algebraic Expressions:

When performing addition or subtraction, we can perform the operations only for the like terms. Let us understand it by an example:

**Example 1:** Add  $7x + y + 7$  to  $3x + 2y + 1$ .

**Solution:** Write down both the given expression into separate rows such that like terms fall below each other

$$\begin{array}{r} 7x + y + 7 \\ + 3x + 2y + 1 \\ \hline 10x + 3y + 8 \end{array} \text{ Ans.}$$

**Example 2:** Subtract  $2x^2 + 5xy + 1$  from  $7x^2 + 2xy + 2y + 3$ .

**Solution:**

$$\begin{array}{r} 7x^2 + 2xy + 2y + 3 \\ - 2x^2 + 5xy + 1 \\ \hline 5x^2 - 3xy + 2y + 2 \end{array} \text{ Ans}$$

**Example 3:** Add  $a - b + ab$ ,  $b - c + bc$  and  $c - a + ac$ .

**Solution:**

$$\begin{array}{r} a - b + ab \\ + \quad b \quad -c + bc \\ + \quad -a \quad c + \quad + ac \\ \hline ab \quad + bc \quad + ac \end{array} \text{ Ans}$$

**Example 4:** Subtract  $4a^2b - 3ab + 5ab^2 - 8a + 7b - 10$  from  $18 - 3a - 11b + 5ab - 2ab^2 + 5a^2b$ .

**Solution:**

$$\begin{array}{r} 18 - 3a - 11b + 5ab - 2ab^2 + 5a^2b \\ - 10 - 8a - 7b - 3ab + 5ab^2 + 4a^2b \\ \hline 28 + 5a - 4b + 8ab - 7ab^2 + a^2b \end{array} \text{ Ans}$$

### Multiplication of Algebraic Expressions:

**(i) Take note of following points for like terms:**

- (a) The coefficients will get multiplied.
- (b) The power of the resultant variable will be the addition of the individual powers.

**Example 1:** Product of  $2x$  and  $3x$  will be  $6x^2$ .

**Example 2:** Product of  $2x$ ,  $3x$  and  $4x$  will be  $24x^3$ .

**(ii) Take note of following points for unlike terms:**

- (a) The coefficients will get multiplied.
- (b) If all the variables are different then there will be no change in the power of variables.
- (c) If some of the variables are same then the respective power of variables will be added.

**Example 1:** Product of  $2x$  and  $3y$  will be  $6xy$ .

**Example 2:** Product of  $2x$ ,  $3y$  and  $4z$  will be  $24xyz$ .

**Example 3:** Product of  $2x^2$ ,  $3x$  and  $4y$  will be  $24x^3y$ .

## **1. Multiplying a Monomial by a Monomial:**

### **(a) Multiplication of two monomials:**

Let us look at some examples:

**Example 1:** Multiplication of terms  $4$  and  $y$  will be  $4y$ .

**Example 2:** Multiplication of terms  $4x$  and  $3y$  will be  $12xy$ .

**Example 3:** Multiplication of terms  $4x$  and  $x$  will be  $4x^2$ .

### **(b) Multiplication of three or more monomials:**

Let us look at some examples:

**Example 1:** Multiplication of terms  $4$ ,  $x$ , and  $y$  will be  $4xy$ .

**Example 2:** Multiplication of terms  $4x$ ,  $3y$ ,  $2$  and  $z$  will be  $24xyz$ .

**Example 3:** Multiplication of terms  $4x^3$ ,  $x^4$ ,  $y^4$  and  $2y$  will be  $8x^7y^5$ .

## **2. Multiplying a Monomial by a Polynomial:**

### **(a) Multiplication of Monomial by a Binomial**

Let us look at some examples:

**Example 1:** Multiplication of  $4$  and  $(x + y)$  will be  $(4x + 4y)$ .

**Example 2:** Multiplication of  $5x$  and  $(3y + 2)$  will be  $(15xy + 10x)$ .

**Example 3:** Multiplication of  $7x^3$  and  $(2x^4 + y^4)$  will be  $(14x^7 + 7x^3y^4)$ .

### **(b) Multiplication of Monomial by a Binomial:**

Let us look at some examples:

**Example 1:** Multiplication of  $4$  and  $(x + y + z)$  will be  $(4x + 4y + 4z)$ .

**Example 2:** Multiplication of  $2x$  and  $(2x + y + z)$  will be  $(4x^2 + 2xy + 2xz)$ .

**Example 3:** Multiplication of  $7x^3$  and  $(2x^4 + y^4 + 2)$  will be  $(14x^7 + 7x^3y^4 + 14x^3)$ .

### Examples based on Multiplying a Monomial by a Polynomial:

**Example 1:** Simplify  $2a(4a - 2) + 7$  and find its values for a)  $x = 2$       b)  $x = 1/2$

**Solution:** On simplifying,  $2a(4a - 2) + 7$ , we get,  $8a^2 - 4a + 7$

(a) For  $x = 2$ ,  $8a^2 - 4a + 7 = 8(2)^2 - 4(2) + 7$   
 $= 31$

(b) For  $x = 1/2$ ,  $8a^2 - 4a + 7 = 8(1/2)^2 - 4(1/2) + 7$   
 $= 7$

**Example 2:** Multiply  $(5/7 \times ab)$  and  $(-21/10 \times a^2b^2)$ .

**Solution:**  $(5/7 \times ab) \times (-21/10 \times a^2b^2) = (5/7) \times (-21/10) \times ab \times a^2b^2$   
 $= (-3/2) a^3b^3$

### 3. Multiplying a Polynomial by a Polynomial:

#### (a) Multiplication of Binomial by a Binomial:

Let us look at some examples:

**Example 1:** Multiplication of  $(4x + y)$  and  $(x + y)$  will be  $(4x^2 + 5xy + y^2)$ .

**Example 2:** Multiplication of  $(5x^2 + 3y)$  and  $(3y + 2)$  will be  $(15x^2y + 10x^2 + 9y^2 + 6y)$ .

#### (b) Multiplication of Binomial by a Trinomial:

Let us look at some examples:

**Example 1:** Multiplication of  $(4x + 2)$  and  $(x + y + z)$  will be  $(4x^2 + 4xy + 4xz + 2x + 2y + 2z)$ .

**Example 2:** Multiplication of  $(2x^2 + 2xy)$  and  $(2x + y + z)$  will be  $(4x^3 + 6x^2y + 2x^2z + 2xy^2 + 2xyz)$ .

### Examples based on Multiplying a Polynomial by a Polynomial

**Example 1:** Multiply the binomials  $(2ab + 3b^2)$  and  $(3ab - 2b^2)$ .

**Solution:**  $(2ab + 3b^2) \times (3ab - 2b^2) = 2ab \times (3ab - 2b^2) + 3b^2 \times (3ab - 2b^2)$   
 $= 6a^2b^2 - 4ab^3 + 9ab^3 - 6b^4$   
 $= 6a^2b^2 + 5ab^3 - 6b^4$

**Example 2:** Simplify  $(a + b + c)(a + b - c)$

**Solution:**  $(a + b + c)(a + b - c) = a(a + b - c) + b(a + b - c) + c(a + b - c)$   
 $= a^2 + ab - ac + ab + b^2 - bc + ac + bc - c^2$   
 $= a^2 + b^2 - c^2 + 2ab$



### Identity:

It is a relation which satisfies  $A = B$ , where  $A$  and  $B$  will contain some variables and for any values of these variables the relation  $A = B$  will always be true.

**Example:** Consider  $(x + 1)(x + 3) = x^2 + 4x + 3$ .

Let us take  $x = 2$ ,

$$\text{LHS} = (2 + 1)(2 + 3) = 3 \times 5 = 15.$$

$$\text{RHS} = 2^2 + 4 \times 2 + 3 = 4 + 8 + 3 = 15.$$

Hence,  $\text{LHS} = \text{RHS}$ .

Similarly, for any values of  $x$  the relation will always be true i.e.  $\text{LHS} = \text{RHS}$ .

### Standard Identities:

$$(i) (a + b)^2 = (a^2 + 2ab + b^2)$$

$$(ii) (a - b)^2 = (a^2 - 2ab + b^2)$$

$$(iii) (a + b)(a - b) = (a^2 - b^2)$$

**Example 1:** Find square of 102.

**Solution:** We can use  $(a + b)^2 = (a^2 + 2ab + b^2)$  identity to simplify the problem.

We can split 102 as  $(100 + 2)$ . Let  $a = 100$  and  $b = 2$ .

Substituting these values in identity, we have,

$$\text{LHS} = (100 + 2)^2 = (102)^2$$

$$\text{RHS} = (100^2 + 2 \times 100 \times 2 + 2^2) = (10000 + 400 + 4) = 10404.$$

Thus, square of 102 is 10404.

**Example 2:** Using  $(x + a)(x + b) = x^2 + (a + b)x + ab$ , find  $105 \times 107$ .

**Solution:** Using given identity, we can write

$$\begin{aligned} 105 \times 107 &= (100 + 5)(100 + 7) \\ &= 100^2 + (5 + 7) \times 100 + 5 \times 7 \\ &= 11235 \end{aligned}$$

**Example 3:** Prove that  $(3a + 7)^2 - 84a = (3a - 7)^2$ .

$$\begin{aligned} \text{LHS} &= (3a + 7)^2 - 84a \\ &= (3a)^2 + 2(3a)(7) + (7)^2 - 84a \\ &= 9a^2 + 42a + 49 - 84a \\ &= 9a^2 - 42a + 49 \end{aligned}$$

$$\begin{aligned} \text{RHS} &= (3a - 7)^2 \\ &= (3a)^2 - 2(3a)(7) + (7)^2 \\ &= 9a^2 - 42a + 49 \end{aligned}$$

Since,  $\text{LHS} = \text{RHS}$ , it is proved that  $(3a + 7)^2 - 84a = (3a - 7)^2$ .

## Previous Years Solution

2019

1<sup>st</sup> Term

(i) Which of the following is a binomial?

(a)  $8x + x$ ; (b)  $12a^2 + 7b + 5c$ ; (c)  $5a \times 7b \times 8c$ ; (d)  $12(a^3 + a)$ .

Ans: (d)  $12(a^3 + a)$ .

(ii)  $3x, 4xy$  are \_\_\_\_\_ terms.

(a) like; (b) unlike; (c) binomial; (d) trinomial.

Ans: (b) unlike

(iii) The sum of  $a + b + ab$ ;  $-b + c - bc$  and  $-c - a + ac$  is:

(a)  $2c + ab - bc + ac$ ; (b)  $ab - bc - ac$ ; (c)  $ab - bc + ac$ ; (d)  $2a + 2b - 2c + ab - ac - bc$ .

Ans: (c)  $ab - bc + ac$

(iv)  $(\frac{1}{2} + \frac{2}{3}) abc = \underline{\hspace{2cm}}$ .

Ans:  $7/6abc$

(v)  $11y^2z - 5y^2z = \underline{\hspace{2cm}}$ .

Ans:  $6y^2z$

(iii) The terms having different variable parts are called unlike terms.

Ans: True

(iv) A binomial is a sum or difference of two monomials.

Ans: True

(v) Dividend = Divisor  $\times$  Quotient + Remainder.

Ans: True

(i)  $x-2y+3z$

c) trinomial

(i) Add:  $4a-6c+2b$ ,  $2a+12c$  and  $-8b+5c$ .

Ans:  $6a-6b+11c$

(ii) Find the product of  $-7x^2y$  and  $5x^3y^3$ .

Ans:  $-35x^5y^4$

(i) Simplify:  $5x+3-[2x-\{x-3(5x-6)\}]$

Ans:  $5x+3-[2x-\{x-3(5x-6)\}]$

$= 5x+3-[2x-\{x-15x+18\}]$

$= 5x+3-[2x-x+15x-18]$

$= 5x+3-2x+x-15x+18$

$= -11x+21$

(i) Simplify:  $3m - 2(m + 3) + 4(m - 1)$

Ans:  $3m - 2(m + 3) + 4(m - 1)$

$= 3m - 2m - 6 + 4m - 4$

$= 5m - 10$

$= 5(m - 2)$

(ii) Divide:  $6x^3 - x + 19x^2 - 29$  by  $2x + 3$ .

Ans:  $6x^3 - x + 19x^2 - 29$  by  $2x + 3$ .

Let us arrange the dividend in descending powers of  $x$ .

$6x^3 + 19x^2 - x - 29$  by  $2x + 3$

The quotient is  $3x^2 + 5x - 8$  with a remainder of  $-5$ .

OR

Divide:  $2x^2 - 11x + 12$  by  $x - 4$ .

Ans: The quotient is  $2x - 3$  and remainder is  $0$ .

(iii) Simplify:  $(a + 1)(a + 2)(a + 3)$ .

Ans:  $(a + 1)(a + 2)(a + 3)$

$= (a + 1) \{(a + 2)(a + 3)\}$

$= (a + 1) \{a^2 + 3a + 2a + 6\}$

$= (a + 1) \{a^2 + 5a + 6\}$

$= (a^3 + 5a^2 + 6a) + (a^2 + 5a + 6)$

$= a^3 + 6a^2 + 11a + 6$

## 2<sup>nd</sup> Term

ii) The sum of  $a+b+ab$ ,  $-b+c-bc$  and  $-c-a+ac$  is

c)  $ab-bc+ac$

iii) Which of the following is a binomial?

d)  $12(a^3 + a)$

iv) The length and breadth of a rectangle are  $(x+8)$  and  $(x-9)$  Units respectively. Then area of the rectangle is

b)  $x^2 - x - 72$

i) A trinomial is the sum or difference of three monomials.

i) Multiply:  $(5x-9y)$  and  $(3x+11y)$  Ans-  $15x^2+28xy-99y^2$ .

ii) Subtract :  $a-b+c$  from  $2a+b-c$  Ans-  $a+2b-2c$ .

i) Divide  $6x^3 - x + 19x^2 - 29$  by  $2x + 3$ . Ans- Q- $3x^2+5x-8$  and R=  $-5$ .

## 3<sup>rd</sup> Term

i) Which of the following is a binomial?

a)  $8x+x$

b)  $12a^2+7b+5c$

c)  $5a \times 7b \times 8c$

d)  $12(a^3 + a)$

Ans: d)  $12(a^3 + a)$

ix) The degree of  $8a^3b^5 + a^2b^2$  is \_\_\_\_\_.

Ans: 8

x) If  $a=2$ ,  $b=1$  and  $c=10$  then find the value of  $3b(a^3-c)$

Ans: (-6)

iv) Subtract  $a-b+c$  from  $2a+b-c$ .

Ans:  $(2a+b-c)-(a-b+c)$

$$= 2a+b-c-a+b-c$$

$$= a+2b-2c$$

ij) What must be added to  $3a^3-4a+6$  to get  $7a^3-4a^2+10a-6$

$$\text{Ans: } (7a^3-4a^2+10a-6) - (3a^3-4a+6)$$

$$= 4a^3-4a^2+14a-12$$

i) Simplify  $8x^3y + 7x^2y(3x-4y) + 2xy(-3x^2+4y)$

$$\text{Ans: } 8x^3y + 21x^3y - 28x^2y^2 - 6x^3y + 8xy^2$$

$$= 23x^3y - 28x^2y^2 + 8xy^2$$

ii) Divide  $x^4 + x^3 - 2x^2 + 4x - 10$  by  $(x-2)$

$$\text{Ans: Quotient} = x^3 + 3x^2 + 4x + 12 \text{ and Remainder} = 14$$

2018

1<sup>st</sup> Term

i) Degree of this polynomial  $3x^7 + 15 + x - 2x^{10}$  is

b) 10

ii) Arranging  $8x^2 - 3x^4 - 12 + 6x^3$  in order of decreasing degree in  $x$  we get  $-3x^4 + 6x^3 + 8x^2 -$

$\frac{12}{\dots}$

i)  $\frac{x}{y} - 2x^3 + 4x^4y^2 - 7$  is a polynomial. False

v) In a polynomial exponents of the variables are always positive integers. True

(i) Add:  $8a - 3b$  and  $2a + 6b$ .

(ii) Find the product of  $-8x^2y$  and  $3x^3y^3$ .

$$(i) (8a - 3b) + (2a + 6b)$$

$$= 10a + 3b.$$

$$(ii) -8x^2y \times 3x^3y^3$$

$$= -24x^5y^4$$

(i) Divide:  $-54x^4y^3z$  by  $6x^2y^2z$ .

$$(i) \frac{-54x^4y^3z}{6x^2y^2z} = -9x^2y.$$

(i) Simplify:  $5x + 3 - [2x - \{x - 3(5x - 6)\}]$

(ii) Divide:  $2x^2 - 11x + 12$  by  $x - 4$ .

Or

Divide:  $x^3 - 8$  by  $x - 2$ ,  $x \neq 2$ .

$$(i) 5x + 3 - [2x - \{x - 3(5x - 6)\}]$$

$$= 5x + 3 - [2x - \{x - 15x + 18\}]$$

$$= 5x + 3 - [2x - x + 15x - 18]$$

$$= 5x + 3 - [16x - 18]$$

$$= 5x + 3 - 16x + 18$$

$$= -11x + 21$$

$$(ii) \begin{array}{r} x-4 \overline{) 2x^2-11x+12} \\ \underline{2x^2-8x} \phantom{+12} \\ (-) \phantom{2x^2-} 3x+12 \\ \underline{-3x+12} \\ \phantom{2x^2-11x+} 0 \end{array}$$



## Exercise Problems

### Question 1

Identify the terms, their coefficients for each of the following expressions.

- (i)  $xyz^2 + 3xy$
- (ii)  $1 - x - 2x^2$
- (iii)  $4p^2q^2 - 4p^2q^2r^2 + r^2$
- (iv)  $4 - xy + yz - xz$
- (v)  $(x/4) - (y/5) - y$
- (vi)  $1.3a - 2.6ab + 1.5b$

### Question 2

Classify the following polynomials as monomials, binomials, trinomials. Which polynomials do not fit in any of these three categories?

- a)  $x^2 + y^2$
- b)  $1000 - x$
- c)  $x + x^2 + x^3 + x^4 + x^5$
- d)  $8 - y - 5x$
- e)  $2y - 3y^2$
- f)  $2y - 3y + 4y^3$
- g)  $5x - 8y + 3xy$
- h)  $4 - 15z^2$
- i)  $ab + bc + cd + da + 2ab$
- j)  $pqr + 2pq + 5pqr$
- k)  $p^2q + pq^2$
- l)  $2p + 2q + 1$

### Question 3

Add the following.

- (i)  $ab - bc + ac, bc - ca + ab, ca - ab - 2bc$
- (ii)  $p - q + pq, q - r + qr, r - p + pr, p + q + r$
- (iii)  $2p^2q^2 - 3pq + 4, 5 + 7pq - 3p^2q^2, 4p^2q^2 + 10pq$
- (iv)  $a^2 + b^2, b^2 + c^2, c^2 + a^2, 2ab + 2bc + 2ac$

### Question 4.

- (a) Subtract  $8a - 7ab + 3b - 20$  from  $20a - 9ab + 5b - 20$
- (b) Subtract  $3pq + 5qr - 7pr + 1$  from  $-4pq + 2qr - 2pr + 5pqr + 1$
- (c) Subtract  $4p^2q - 4pq - 5pq^2 - 8p + 7q - 18$  from  $18 - 3p - 11q + 5pq - 2pq^2 + 5p^2q$

### Question 5

What are the coefficient of each term in the below expression?

$$4p^2q^2 + 4p^2q^2r^2 - r^2 + 5$$

- a)  $4, 4, -1, 5$
- b)  $4, 4, 1, 5$
- c)  $4, 4r^2, -r^2, 5$
- d) None of these

### Question 6

The product of a monomial and trinomial will be a

- a) monomial
- b) trinomial
- c) binomial
- d) None of these

### Question 7

The exponents of a variable term in the polynomial is a

- a) integers
- b) negative integers
- c) positive integers
- d) non -negative integers

**Question 8**

The expression  $pqr + rqp + qpr$  is a

- a) Monomial
- b) trinomial
- c) binomial
- d) none of these

**Question 9**

Find the product of the following expression

- (a)  $11, 7x$
- (b)  $-4x, y$
- (c)  $-4p, pq, pr$
- (d)  $4p^3, -3p, p^2$
- (e)  $3mn, 4n$
- (f)  $51p, p^2, p^8$
- (g)  $2p, 4q, 8r$
- (h)  $xy, 2x^2y, 2xy^2, xy$
- (i)  $a, 2b, 3c$
- (j)  $xy, yz, zx$
- (k)  $2, 4y, 8y^2, 16y^3$
- (l)  $a, 2b, 3c, 6abc$
- (m)  $p, -pq, pqr$

**Question 10**

Volume of the cuboid with Length as  $2x$ , breath as  $2y$  and Height as  $2z$  is given by

- a)  $xyz$
- b)  $8xyz$
- c)  $2x+2y+2z$
- d) None of these

**Question 11**

The sum of area of the squares of side  $2a$  and  $2b$  will be

- a)  $2a+ 2b$
- b)  $4a^2 + 4b^2$
- c)  $ab$
- d) None of these

**Question 12**

Identify the terms, their coefficients for each of the following expressions.

- (i)  $xyz^2 + 3xy$
- (ii)  $1 - x - 2x^2$
- (iii)  $4p^2q^2 - 4p^2q^2r^2 + r^2$
- (iv)  $4 - xy + yz - xz$
- (v)  $(x/4) - (y/5) - y$
- (vi)  $1.3a - 2.6ab + 1.5b$

**Question 13**

Classify the following polynomials as monomials, binomials, trinomials. Which polynomials do not fit in any of these three categories?

- $x^2 + y^2$
- $1000-x$
- $x + x^2 + x^3 + x^4 + x^5$

$8 - y + -5x$   
 $2y - 3y^2$   
 $2y - 3y + 4y^3$   
 $5x - 8y + 3xy$   
 $4 - 15z^2$   
 $ab + bc + cd + da + 2ab$   
 $pqr + 2pq + 5pqr$   
 $p^2q + pq^2$   
 $2p + 2q + 1$

**Question 14**

Add the following.

- (i)  $ab - bc + ac, bc - ca + ab, ca - ab - 2bc$   
(ii)  $p - q + pq, q - r + qr, r - p + pr, p + q + r$   
(iii)  $2p^2q^2 - 3pq + 4, 5 + 7pq - 3p^2q^2, 4p^2q^2 + 10pq$   
(iv)  $a^2 + b^2, b^2 + c^2, c^2 + a^2, 2ab + 2bc + 2ac$

**Question 15**

- (a) Subtract  $8a - 7ab + 3b - 20$  from  $20a - 9ab + 5b - 20$   
(b) Subtract  $3pq + 5qr - 7pr + 1$  from  $-4pq + 2qr - 2pr + 5pqr + 1$   
(c) Subtract  $4p^2q - 4pq - 5pq^2 - 8p + 7q - 18$  from  $18 - 3p - 11q + 5pq - 2pq^2 + 5p^2q$

**Question 16**

What are the coefficient of each term in the below expression?

$4p^2q^2 + 4p^2q^2r^2 - r^2 + 5$

- a) 4,4,-1,5  
b) 4,4,1,5  
c)  $4, 4r^2, -r^2, 5$   
d) None of these

**Question 17**

The product of a monomial and trinomial will be a

- a) monomial  
b) trinomial  
c) binomial  
d) None of these

**Question 18**

The exponents of a variable term in the polynomial is a

- a) integers  
b) negative integers  
c) positive integers  
d) non -negative integers

**Question 19**

The expression  $pqr + rqp + qpr$  is a

- a) Monomial  
b) trinomial  
c) binomial  
d) none of these

**Question 20**

Use a suitable identity to get each of the following products.

- a)  $(p - 11)(p + 11)$   
b)  $(2y + 5)(2y - 5)$   
c)  $(12a - 9)(12a + 9)$   
d)  $(2a - 1/2)(2a + 1/2)$   
e)  $(1.1m - 0.4)(1.1m + 0.4)$   
f)  $(a^2 + b^2)(-a^2 + b^2)$

- g)  $(6x - 7)(6x + 7)$
- h)  $(-a/2 + c/2)(-a/2 + c/2)$
- i)  $[(p/8) + (3q/4)][(p/8) + (3q/4)]$
- j)  $(3a + 9b)(3a - 9b)$
- k)  $2(a - 9)^2$
- l)  $5(xy - 3z)^2$
- m)  $(6x + 5y)^2$
- n)  $36[(3p/2) + (2q/3)]^2$
- o)  $(x - 0.5y)^2$
- p)  $(2xy - 5y)^2$

### Question 21

Use the identity  $(x + a)(x + b) = x^2 + (a + b)x + ab$  to find the following products.

- (i)  $(p + 10)(p + 11)$
- (ii)  $(4x + 9)(4x + 12)$
- (iii)  $(x - 5)(x - 1)$
- (iv)  $(9x - 5)(9x - 1)$
- (v)  $(2x + 5y)(2x + 3y)$
- (vi)  $(2a^2 + 9)(2a^2 + 5)$

### Question 22

Simplify the following

- (i)  $(x^2 - y^2)^2 + 4x^2y^2$
- (ii)  $(p + q)^2 - (p - q)^2 + p^2q^2$
- (iii)  $(2m - 8n)^2 + (2m + 8n)^2$
- (iv)  $(4m + 5n)^2 + (5m + 4n)^2 + (4m + 5n)(4m - 5n)$
- (v)  $(.5p - 1.5q)^2 - (.5p - 1.5q)^2 + p^2q^2$
- (vi)  $(ab - bc)^2 + 2ab^2c$
- (vii)  $(m^2 - n^2m)^2 + 2m^2n^2$

### Question 23

Using identities, evaluate.

- a)  $91^2$
- b)  $89^2$
- c)  $202^2$
- d)  $999^2$
- e)  $1.2^2$
- f)  $397 \times 403$
- g)  $48 \times 52$
- h)  $5.1^2$
- i)  $61^2 - 59^2$
- j)  $11.1^2 - 9.9^2$
- k)  $503 \times 504$
- l)  $2.1 \times 2.2$
- m)  $103 \times 98$
- n)  $9.7 \times 9.8$
- o)  $729^2 - 271^2$

### Question 24

Find the value of x if  $8x = 35^2 - 27^2$

### Question 25

- a) If  $a - 1/a = 4$ , find the value of  $a^2 + 1/a^2$
- b) If  $p + q = 13$  and  $pq = 22$ , then  $p^2 + q^2$