## ST. LAWRENCE HIGH SCHOOL

A JESUIT CHRISTIAN MINORITY INSTITUTION

- Subject- Physics

Study Material -4
Class IX

- Date : 8.05.2020
- Chapter: Motion (Numericals)

Question 1: Calculate the force needed to speed up a car with a rate of $5 \mathrm{~ms}^{-2}$, if the mass of the car is 1000 kg .

Solution: According to question:
Acceleration $(\mathrm{a})=5 \mathrm{~m} / \mathrm{s} 2=5 \mathrm{~m} / \mathrm{s} 2$ and Mass $(\mathrm{m})=1000 \mathrm{~kg}$, therefore, Force $(\mathrm{F})=$ ?
We know that, $\mathrm{F}=\mathrm{m} \times \mathrm{aF}=\mathrm{m} \times \mathrm{a}$
$=1000 \mathrm{~kg} \times 5 \mathrm{~m} / \mathrm{s} 2=1000 \mathrm{~kg} \times 5 \mathrm{~m} / \mathrm{s} 2$
$=5000 \mathrm{~kg} \mathrm{~m} / \mathrm{s} 2=5000 \mathrm{~kg} \mathrm{~m} / \mathrm{s} 2$
Therefore, required Force $=5000 \mathrm{~m} / \mathrm{s} 2=5000 \mathrm{~m} / \mathrm{s} 2$ or 5000 N

Question 2: If the mass of a moving object is 50 kg , what force will be required to speed up the object at a rate of $2 \mathrm{~ms}^{-2}$ ?

Solution: According to the question;

Acceleration $(\mathrm{a})=2 \mathrm{~ms}-2=2 \mathrm{~ms}-2$ and Mass $(\mathrm{m})=50 \mathrm{~kg}$, therefore, Force $(\mathrm{F})=$ ?
We know that, $\mathrm{F}=\mathrm{m} \times \mathrm{aF}=\mathrm{m} \times \mathrm{a}$
$=50 \mathrm{~kg} \times 2 \mathrm{~m} / \mathrm{s} 2=50 \mathrm{~kg} \times 2 \mathrm{~m} / \mathrm{s} 2$
$=100 \mathrm{~kg} \mathrm{~m} / \mathrm{s} 2=100 \mathrm{~kg} \mathrm{~m} / \mathrm{s} 2$
Therefore, required Force $=100 \mathrm{~m} / \mathrm{s} 2=100 \mathrm{~m} / \mathrm{s} 2$ or 100 N
Question 3: To accelerate a vehicle to $3 \mathrm{~m} / \mathrm{s}^{2}$ what force will be needed if the mass of the vehicle is equal to 100 kg ?

Solution: According to the question:
Acceleration $(\mathrm{a})=3 \mathrm{~m} / \mathrm{s} 2=3 \mathrm{~m} / \mathrm{s} 2$ and Mass $(\mathrm{m})=100 \mathrm{~kg}$, therefore, Force $(\mathrm{F})=$ ?
We know that, $\mathrm{F}=\mathrm{m} \times \mathrm{aF}=\mathrm{m} \times \mathrm{a}$
$=100 \mathrm{~kg} \times 3 \mathrm{~m} / \mathrm{s} 2=100 \mathrm{~kg} \times 3 \mathrm{~m} / \mathrm{s} 2$
$=300 \mathrm{~kg} \mathrm{~m} / \mathrm{s} 2=300 \mathrm{~kg} \mathrm{~m} / \mathrm{s} 2$
Therefore, required Force $=300 \mathrm{~m} / \mathrm{s} 2=300 \mathrm{~m} / \mathrm{s} 2$ or 300 N

## Question 4.

A particle of 10 kg is moving in a constant acceleration $2 \mathrm{~m} / \mathrm{s}^{2}$ starting from rest. What is its momentum and velocity per the table given below

| S.No | time | Momentum | Velocity |
| :--- | :--- | :--- | :--- |
| 1 | 1 sec |  |  |
| 2 | 1.5 sec |  |  |
| 3 | 2 sec |  |  |
| 4 | 2.5 sec |  |  |

## Solution

Velocity can find using
$v=u+a t v=u+a t$
For $u=0$
v=atv=at
Momentum
$\mathrm{P}=\mathrm{mvP}=\mathrm{mv}$

| S.No | time | Momentum | Velocity |
| :--- | :--- | :--- | :--- |
| 1 | 1 sec | $20 \mathrm{Kg} \mathrm{m} / \mathrm{s}$ | $2 \mathrm{~m} /$ |
| 2 | 1.5 sec | $30 \mathrm{~kg} \mathrm{~m} / \mathrm{s}$ | $3 \mathrm{~m} / \mathrm{s}$ |
| 3 | 2 sec | $40 \mathrm{~kg} \mathrm{~m} / \mathrm{s}$ | $4 \mathrm{~m} / \mathrm{s}$ |
| 4 | 2.5 sec | $50 \mathrm{~kg} \mathrm{~m} / \mathrm{s}$ | $5 \mathrm{~m} / \mathrm{s}$ |

## Question 5

If a net force of 7 N was constantly applied on 400 g object at rest, how long will it take to raise its velocity to $80 \mathrm{~m} / \mathrm{s}$ ?
a. 0 s
b. 2.23 s
c. 3.47 s
d. 4.57 s

## Solution

Given $\mathrm{F}=7 \mathrm{~N}, \mathrm{~m}=400 \mathrm{~g}=.4 \mathrm{~kg}$ Acceleration is given by $\mathrm{a}=\mathrm{Fma}=\mathrm{Fm}$
$a=17.5 \mathrm{~m} / \mathrm{s}^{2}$

Now $u=0, v=80 \mathrm{~m} / \mathrm{s} \mathrm{v}=\mathrm{u}+\mathrm{atv}=\mathrm{u}+\mathrm{at}$
$\mathrm{t}=\mathrm{v}$-uat=v-ua
$t=4.57 \mathrm{sec}$

## Question 6

A sedan car of mass 200 kg is moving with a certain velocity. It is brought to rest by the application of brakes, within a distance of 20 m when the average resistance being offered to it is 500 N . What was the velocity of the motor car?

## Solution

$\mathrm{F}=\mathrm{maF}=\mathrm{ma}$
or
$\mathrm{a}=\mathrm{Fm} \mathrm{a}=\mathrm{Fm}$
or
$a=-500 / 200=-2.5 \mathrm{~m} / \mathrm{s}^{2}$
Now
v2=u2+2asv2=u2+2as
Now $v=0, \mathrm{~s}=20 \mathrm{~m}, \mathrm{a}=-2.5 \mathrm{~m} / \mathrm{s}^{2}$
So, $u=10 \mathrm{~m} / \mathrm{s}$

## Question 7

A driver accelerates his car first at the rate of $4 \mathrm{~m} / \mathrm{s}^{2}$ and then at the rate of $8 \mathrm{~m} / \mathrm{s}^{2}$. Calculate the ration of the forces exerted by the engines?

## Solution

$\mathrm{F}_{1}=\mathrm{ma} \mathrm{F}^{\mathrm{F}} 1=\mathrm{ma} 1$
and
$\mathrm{F}_{2}=\mathrm{ma2F}$ 2=ma2
So, Ratio of force exerted is given by
$=\mathrm{F}_{1} \mathrm{~F}_{2}=$ ma1ma2 $=\mathrm{a}_{1 \mathrm{a} 2}=1: 2=\mathrm{F} 1 \mathrm{~F} 2=\mathrm{ma} 1 \mathrm{ma} 2=\mathrm{a} 1 \mathrm{a} 2=1: 2$

## Question 8

An object of mass 10 g is sliding with a constant velocity of $2 \mathrm{~m} / \mathrm{s}$ on a frictionless horizontal table. The force required to keep the object moving with the same velocity is
(a) 0 N
(b) 5 N
(c) 10 N
(d) 20 N

## Solution

As $m=0, F=0$
Hence (a) is correct

## Question 9

A cricket ball of mass 0.20 kg is moving with a velocity of $1.2 \mathrm{~m} / \mathrm{s}$. Find the impulse on the ball and average force applied by the player if he is able to stop the ball in 0.10 s?

## Solution

Impulse $=$ Change in momentum
$\mathrm{I}=\Delta \mathrm{p}=\mathrm{m} \Delta \mathrm{v}=.20 \times 1.2=.12 \mathrm{I}=\Delta \mathrm{p}=\mathrm{m} \Delta \mathrm{v}=.20 \times 1.2=.12 \mathrm{Kgm} / \mathrm{s}$
Now
Impulse is also defined as
$\mathrm{I}=\mathrm{F} \times \mathrm{tl}=\mathrm{F} \times \mathrm{t}$
or
$\mathrm{F} \times \mathrm{t}=.12 \mathrm{~F} \times \mathrm{t}=.12$
or
$\mathrm{F}=.12 .10=1.2 \mathrm{~F}=.12 .10=1.2 \mathrm{~N}$

## Question 10

A car start from rest and acquire a velocity of $54 \mathrm{~km} / \mathrm{h}$ in 2 sec . Find
(i) the acceleration
(ii) distance travelled by car assume motion of car is uniform
(iii) If the mass of the car is 1000 Kg , what is the force acting on it?

## Solution

Given $u=0, v=54 \mathrm{~km} / \mathrm{hr}=15 \mathrm{~m} / \mathrm{s}, \mathrm{t}=2 \mathrm{sec} \mathrm{a}$. Acceleration is given by
$a=\Delta v t a=\Delta v t$
So, $a=7.5 \mathrm{~m} / \mathrm{s}^{2}$
b. Distance is given by
s=ut+12at2s=ut+12at2
$\mathrm{s}=15 \mathrm{~m}$
c. Force is given by $\mathrm{F}=\mathrm{ma}=1000 \times 7.5=7500 \mathrm{~F}=\mathrm{ma}=1000 \times 7.5=7500 \mathrm{~N}$

## Question 11

A hockey ball of mass .2 Kg travelling at $10 \mathrm{~ms}^{-1}$ is struck by a hockey stick so as to return it along its original path with a velocity at $2 \mathrm{~m} / \mathrm{s}$. Calculate the change of momentum occurred in the motion of the hockey ball by the force applied by the hockey stick.

## Solution

$\Delta \mathrm{P}=\mathrm{m} \times(\mathrm{v}-\mathrm{u})=0.2 \times(-2-10)=-2.4 \Delta \mathrm{P}=\mathrm{m} \times(\mathrm{v}-\mathrm{u})=0.2 \times(-2-10)=-2.4 \mathrm{~kg} \mathrm{~ms}^{-1}$ (The negative sign indicates a change in direction of hockey ball after it is struck by hockey stick. )

## Question 12

Two objects of masses of 100 gm and 200 gm are moving in along the same line and direction with velocities of $2 \mathrm{~ms}^{-1}$ and $1 \mathrm{~ms}^{-1}$ respectively. They collide and after collision, the first object moves at a velocity of $1.67 \mathrm{~ms}^{-1}$. Determine the velocity of the second object?

## Solution

Given $\mathrm{m} 1=100 \mathrm{gm}=0.1 \mathrm{kgm} 1=100 \mathrm{gm}=0.1 \mathrm{~kg}, \mathrm{~m} 2=200 \mathrm{gm}=0.2 \mathrm{kgm} 2=200 \mathrm{gm}$ $=0.2 \mathrm{~kg}$
$\mathrm{u}_{1}=2 \mathrm{u} 1=2 \mathrm{~ms}^{-1}, \mathrm{u} 2=1 \mathrm{u} 2=1 \mathrm{~ms}^{-1}, \mathrm{v} 1=1.67 \mathrm{v} 1=1.67 \mathrm{~ms}^{-1}, \mathrm{v} 2=? \mathrm{v} 2=$ ?
By the law of conservation of momentum,
m1u1+m2u2 $=\mathrm{m}_{1} \mathrm{v} 2+\mathrm{m} 2 \mathrm{v} 2 \mathrm{~m} 1 \mathrm{u} 1+\mathrm{m} 2 \mathrm{u} 2=\mathrm{m} 1 \mathrm{v} 2+\mathrm{m} 2 \mathrm{v} 2$
$0.1 \times 2+0.2 \times 1=0.1 \times 1.67+0.2 \mathrm{v} 20.1 \times 2+0.2 \times 1=0.1 \times 1.67+0.2 \mathrm{v} 2$
$\mathrm{v} 2=1.165 \mathrm{v} 2=1.165 \mathrm{~ms}^{-1}$
It will move in the same direction after collision

## Question 13

Velocity versus time graph of a ball of mass 100 g rolling on a concrete floor is shown below.
Calculate the acceleration and the frictional force of the floor on the ball?


Solution
From the graph ,we can see that
$\Delta \mathrm{v}=-80 \mathrm{~m} / \mathrm{s} \Delta \mathrm{v}=-80 \mathrm{~m} / \mathrm{s}, \mathrm{t}=8 \mathrm{sec}$
Now
$\mathrm{a}=\Delta \mathrm{vt}=-10 \mathrm{~m} / \mathrm{s} 2 \mathrm{a}=\Delta \mathrm{vt}=-10 \mathrm{~m} / \mathrm{s} 2$
Frictional force will be given as
$\mathrm{F}=\mathrm{ma}=.1 \times-10=-1 \mathrm{NF}=\mathrm{ma}=.1 \times-10=-1 \mathrm{~N}$

## Question 14

An object of mass 1 kg acquires a speed of $10 \mathrm{~m} / \mathrm{s}$ when pushed forward. What is the impulse given to the object?

## Solution

Impulse=Change in Momentum $=10 \mathrm{Kgm} / \mathrm{s}$

## Question 15

A bullet of mass 10 gm is fired with an initial velocity of $20 \mathrm{~m} / \mathrm{s}$ from a rifle of mass 4 kg . Calculate the initial recoil velocity of the rifle?

## Solution

Let v be the initial recoil velocity of the rifle From law of conservation of Momentum
$0=.01 \times 20+4 \times v 0=.01 \times 20+4 \times v$
Or v=-.05m/sv=-.05m/s

