



ST. LAWRENCE HIGH SCHOOL
A JESUIT CHRISTIAN MINORITY INSTITUTION



STUDY MATERIAL-2
SUBJECT – MATHEMATICS
Pre-test

Chapter: MATRICES AND DETERMINANTS

Class: XII

Topic: MATRICES

Date: 09.05.2020

PART 2

EXERCISE SET 1

1. If $A(\alpha, \beta) = \begin{bmatrix} \cos \alpha & \sin \alpha & 0 \\ -\sin \alpha & \cos \alpha & 0 \\ 0 & 0 & e^\beta \end{bmatrix}$, then $A(\alpha, \beta)^{-1}$ is equal to
 (a) $A(-\alpha, -\beta)$ (b) $A(-\alpha, \beta)$
 (c) $A(\alpha, -\beta)$ (d) $A(\alpha, \beta)$
2. If $\begin{bmatrix} \alpha & \beta \\ \gamma & -\alpha \end{bmatrix}$ is to be the square root of a two-rowed unit matrix, then α, β and γ should satisfy the relation
 (a) $1 + \alpha^2 + \beta\gamma = 0$ (b) $1 - \alpha^2 - \beta\gamma = 0$
 (c) $1 - \alpha^2 + \beta\gamma = 0$ (d) $\alpha^2 + \beta\gamma - 1 = 0$
3. If $A = \begin{bmatrix} 2 & 14 & 7 \\ 0 & \sin 2x & \cos 2x \\ 0 & \cos 2x & \sin 2x \end{bmatrix}$, then $|A|$ equals
 (a) $\cos 2x$ (b) -2
 (c) $-2 \cos 4x$ (d) $\sin 4x$
4. If A is a matrix such that $A^2 + A + 2I = 0$, then which of the following is **not** true?
 (a) A is symmetric (b) A is non-singular
 (c) $A \neq 0$ (d) $A^{-1} = -\frac{1}{2}(A + I)$
5. If $E(\theta) = \begin{bmatrix} \cos^2 \theta & \cos \theta \sin \theta \\ \cos \theta \sin \theta & \sin^2 \theta \end{bmatrix}$ and θ and ϕ differ by an odd multiple of $\pi/2$, then $E(\theta)E(\phi)$ is
 (a) a null matrix (b) a unit matrix
 (c) a diagonal matrix (d) none of these
6. If $A = [a_{ij}]$ is a 4×4 matrix and C_{ij} is the cofactor of the element a_{ij} in $|A|$, then the expression $a_{11}C_{11} + a_{12}C_{12} + a_{13}C_{13} + a_{14}C_{14}$ is equal to
 (a) 0 (b) -1
 (c) 1 (d) $|A|$
7. If $A = \begin{bmatrix} 0 & c & -b \\ -c & 0 & a \\ b & -a & 0 \end{bmatrix}$ and $B = \begin{bmatrix} a^2 & ab & ac \\ ab & b^2 & bc \\ ac & bc & c^2 \end{bmatrix}$, then $|AB|$ equals
 (a) A^3 (b) B^2
 (c) 1 (d) none of these
8. If A and B are square matrices of the same order such that $A^2 = A, B^2 = B, AB = BA = O$, then
 (a) $(A - B)^2 = B - A$ (b) $(A - B)^2 = A - B$
 (c) $(A + B)^2 = A + B$ (d) none of these
9. If $A = \begin{bmatrix} 2x & 0 \\ x & x \end{bmatrix}$ and $A^{-1} = \begin{bmatrix} 1 & 0 \\ -1 & 2 \end{bmatrix}$, then x equals
 (a) 2 (b) $-(1/2)$
 (c) 1 (d) $1/2$
10. The equations $2x + y = 4, 3x + 2y = 2$ and $x + y = -2$ have
 (a) no solution
 (b) one solution
 (c) two solutions
 (d) infinitely many solutions

24. If a matrix A is such that $3A^3 + 2A^2 + 5A + I = 0$, then A^{-1} is equal to
 (a) $-(3A^2 + 2A + 5I)$ (b) $3A^2 + 2A + 5$
 (c) $3A^2 - 2A - 5$ (d) none of these
25. Given $2x - y + 2z = 2$, $x - 2y + z = -4$ and $x + y + \lambda z = 4$, then the value of λ such that the given system of equations has no solution is
 (a) 3 (b) 1
 (c) 0 (d) -3
26. Assuming that the sums and products given below are defined, then which of the following is not true for matrices?
 (a) $(AB)' = B'A'$
 (b) $A + B = B + A$
 (c) $AB = AC$ does not imply $B = C$
 (d) $AB = 0$ implies $A = 0$ or $B = 0$
27. Which of the following is **not** true?
 (a) $A^2 - B^2 = (A + B)(A - B)$
 (b) $(A^T)^T = A$
 (c) $(AB)^n = A^n B^n$, where A and B commute
 (d) $(A - I)(I + A) = 0 \Leftrightarrow A^2 = 1$
28. If in a square matrix $A = [a_{ij}]$, we find that $a_{ij} = a_{ji} \forall i, j$ then A is a
 (a) symmetric matrix (b) diagonal matrix
 (c) transpose matrix (d) skew-symmetric matrix
29. If A is a non-singular square matrix of order n , then the rank of A is
 (a) equal to n (b) less than n
 (c) greater than n (d) none of these
30. If A and B are square matrices of the order 3, such that $|A| = -1$ and $|B| = 3$, then the value of $|3AB|$ is
 (a) -9 (b) -81
 (c) -27 (d) 81
31. If $A = \begin{bmatrix} 1 & 2 & x \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & -2 & y \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ and $AB = I_3$, then $x + y$ equals
 (a) 0 (b) -1
 (c) 2 (d) none of these
32. If $A = \begin{bmatrix} 1 & 2 \\ 2 & 3 \end{bmatrix}$ and $A^2 - kA - I_2 = 0$, then the value of k is
 (a) 4 (b) 2
 (c) 1 (d) -4
33. If A satisfies the equation $x^3 - 5x^2 + 4x + k = 0$, then A^{-1} exists if
 (a) $k \neq 1$ (b) $k \neq 2$
 (c) $k \neq -1$ (d) none of these
34. If matrix $A = \begin{bmatrix} \alpha & 2 \\ 2 & \alpha \end{bmatrix}$ and $|A^3| = 125$, then the value of α is
 (a) ± 3 (b) ± 2
 (c) ± 5 (d) 0
35. If A is a matrix of order 2×3 and AB is a matrix of order 2×5 , then B may be a
 (a) 3×5 matrix (b) 5×3 matrix
 (c) 3×2 matrix (d) 5×2 matrix
36. Let A and B be two square matrices such that $AB = A$ and $BA = B$, then $A^2 = A$
 (a) B (b) A
 (c) I (d) 0
37. If $AB = A$ and $BA = A$, where A and B are square matrices, then
 (a) $B^2 = B$ and $A^2 = A$ (b) $B^2 \neq B$ and $A^2 = A$
 (c) $A^2 \neq A$ and $B^2 = B$ (d) $A^2 \neq A$ and $B^2 \neq B$
38. If A is an $m \times n$ matrix such that AB and BA are both defined, then B is an
 (a) $m \times n$ matrix (b) $n \times m$ matrix
 (c) $n \times n$ matrix (d) $m \times m$ matrix
39. If the matrix $\begin{bmatrix} (x-a)^2 & (x-b)^2 & (x-c)^2 \\ (y-a)^2 & (y-b)^2 & (y-c)^2 \\ (z-a)^2 & (z-b)^2 & (z-c)^2 \end{bmatrix}$ is a zero matrix, then a, b, c, x, y, z are connected by
 (a) $a + b + c = 0, x + y + z = 0$
 (b) $a + b + c = 0, x = y = z$
 (c) $a = b = c, x + y + z = 0$
 (d) none of these
40. The value of x for which the matrix $A = \begin{bmatrix} 6 & x-2 \\ 3 & x \end{bmatrix}$ has no inverse is
 (a) -2 (b) 2
 (c) 0 (d) 3
41. If $\begin{bmatrix} x+y & 8 \\ 0 & x-y \end{bmatrix} = \begin{bmatrix} 2 & 3 \\ -1 & 5 \end{bmatrix} + \begin{bmatrix} 3 & 5 \\ 1 & -2 \end{bmatrix}$, then (x, y) equals
 (a) (4, 1) (b) (1, 4)
 (c) (-4, -1) (d) (1, -4)
42. If $A = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$ and $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$, then which one of the following holds for all $n \geq 1$, by the principle of mathematical induction?
 (a) $A^n = 2^{n-1}A - (n-1)I$ (b) $A^n = nA - (n-1)I$
 (c) $A^n = 2^{n-1}A + (n-1)I$ (d) $A^n = nA + (n-1)I$

43. If $A = \begin{bmatrix} i & 0 \\ 0 & i \end{bmatrix}$, $n \in N$, then A^{4n} equals
 (a) $\begin{bmatrix} 0 & i \\ i & 0 \end{bmatrix}$ (b) $\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$
 (c) $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ (d) $\begin{bmatrix} 0 & i \\ i & 0 \end{bmatrix}$
44. If A and B are symmetric matrices, then ABA is
 (a) symmetric (b) skew-symmetric
 (c) diagonal (d) triangular
45. If a, b, c are distinct and $\begin{bmatrix} a & a^2 & a^3 - 1 \\ b & b^2 & b^3 - 1 \\ c & c^2 & c^3 - 1 \end{bmatrix} = 0$, then
 (a) $abc = 1$ (b) $a + b + c = 0$
 (c) $a + b + c = 1$ (d) $ab + bc + ca = 0$
46. If $A = \begin{bmatrix} 2 & 3 & 1 \\ 4 & -2 & 6 \end{bmatrix}$, $B = \begin{bmatrix} 0 & 3 & 2 \\ -2 & 1 & 4 \end{bmatrix}$ and $C = \begin{bmatrix} 7 & 8 \\ 9 & 0 \\ 6 & 5 \end{bmatrix}$,
 then $2A + 3B - C^T$ equals
 (a) $\begin{bmatrix} -3 & 6 & 2 \\ -6 & -1 & 19 \end{bmatrix}$ (b) $\begin{bmatrix} 3 & 6 & 2 \\ 6 & 1 & 19 \end{bmatrix}$
 (c) $\begin{bmatrix} 11 & 24 & 14 \\ 10 & 7 & 31 \end{bmatrix}$ (d) none of these
47. If $A^2 - A + I = 0$, then the inverse of A is
 (a) A (b) $A + I$
 (c) $I - A$ (d) $A - I$
48. If ω is a complex cube root of unity, and $A = \begin{bmatrix} \omega & 0 \\ 0 & \omega \end{bmatrix}$,
 then A^{100} is equal to
 (a) A (b) $-A$
 (c) 0 (d) none of these
49. If A = diagonal (d_1, d_2, \dots, d_n), then A^n is
 (a) diag. ($d_1^{n-1}, d_2^{n-1}, \dots, d_n^{n-1}$)
 (b) A
 (c) diag. ($d_1^n, d_2^n, \dots, d_n^n$)
 (d) none of these
50. If $[1 \ x \ 1] \begin{bmatrix} 2 & 3 & 2 \\ 0 & 5 & 1 \\ 0 & 3 & 2 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ x \end{bmatrix} = 0$, then the values of x are
 (a) $1, 8$ (b) $-1, 8$
 (c) $-1, -8$ (d) $1, -8$
51. Let $A = \begin{bmatrix} 1 & -1 & 1 \\ 2 & 1 & -3 \\ 1 & 1 & 1 \end{bmatrix}$ and (10) $B = \begin{bmatrix} 4 & 2 & 2 \\ -5 & 0 & \alpha \\ 1 & -2 & 3 \end{bmatrix}$. If B is the inverse of A , then α is
 (a) -2 (b) -1
 (c) 2 (d) 5
52. If $A^3 = 0$, then $I + A + A^2$ equals
 (a) $I - A$ (b) $(I - A)^{-1}$
 (c) $(I + A)^{-1}$ (d) none of these
53. The inverse of a symmetric matrix is
 (a) symmetric (b) skew-symmetric
 (c) diagonal (d) none of these
54. If $\begin{bmatrix} 2 & -1 \\ 1 & 0 \\ -3 & 4 \end{bmatrix} A = \begin{bmatrix} -1 & -8 & -10 \\ 1 & -2 & -5 \\ 9 & 22 & 15 \end{bmatrix}$, then the matrix A is
 (a) $\begin{bmatrix} 1 & -2 & -5 \\ 3 & 4 & 0 \end{bmatrix}$ (b) $\begin{bmatrix} 1 & 3 \\ -2 & 4 \\ -5 & 0 \end{bmatrix}$
 (c) $\begin{bmatrix} -1 & 2 & 5 \\ 3 & 4 & 0 \end{bmatrix}$ (d) none of these
55. If $A = \begin{bmatrix} a & b \\ b & a \end{bmatrix}$ and $A^2 = \begin{bmatrix} \alpha & \beta \\ \beta & \alpha \end{bmatrix}$, then
 (a) $\alpha = 2ab, \beta = a^2 + b^2$ (b) $\alpha = a^2 + b^2, \beta = ab$
 (c) $\alpha = a^2 + b^2, \beta = 2ab$ (d) $\alpha = a^2 + b^2, \beta = a^2 - b^2$
56. If A is a non-singular matrix of order 3×3 , then $\text{adj}(\text{adj } A)$ is equal to
 (a) $|A|A$ (b) $|A|^2 A$
 (c) $|A|^{-1} A$ (d) none of these
57. If A and B are two square matrices such that $AB = A$ and $BA = B$ then
 (a) A, B are idempotent (b) only A is idempotent
 (c) only B is idempotent (d) none of these
58. The matrices
 $P = \begin{bmatrix} u_1 & v_1 & w_1 \\ u_2 & v_2 & w_2 \\ u_3 & v_3 & w_3 \end{bmatrix}$ and $Q = \frac{1}{9} \begin{bmatrix} 2 & 2 & 1 \\ 12 & -5 & m \\ -8 & 1 & 5 \end{bmatrix}$
 are such that $PQ = I$ (an identity matrix). Solving the equations
 $\begin{bmatrix} u_1 & v_1 & w_1 \\ u_2 & v_2 & w_2 \\ u_3 & v_3 & w_3 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 5 \end{bmatrix}$ the value of y comes out to be -3 . Then the value of m is equal to
 (a) 27 (b) 7
 (c) -27 (d) -7

59. If A is a square matrix such that $A^2 = A$ and $(I + A)^n = I + \lambda A$, then $\lambda = ?$

(a) $(2n - 1)$ (b) $2^n - 1$
 (c) $2n + 1$ (d) none of these

60. If A is skew-symmetric, then A^n for $n \in N$ is

(a) symmetric (b) skew-symmetric
 (c) diagonal (d) none of these

61. If ω is the cube root of unity, then

$$\begin{bmatrix} \omega & \omega^2 \\ 1 & \omega \\ \omega^2 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & \omega & \omega^2 \\ \omega & \omega^2 & 1 \end{bmatrix} \times \begin{bmatrix} 1 \\ \omega \\ \omega^2 \end{bmatrix} \text{ equals}$$

(a) $\begin{bmatrix} \omega - \omega^2 \\ \omega - \omega^2 \\ \omega - 2\omega^2 \end{bmatrix}$ (b) $\begin{bmatrix} 1 \\ \omega \\ \omega^2 \end{bmatrix}$
 (c) $(\omega - \omega^2) \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$ (d) none of these

62. Consider the system of equations in x, y, z as $x \sin 3\theta - y + z = 0$, $x \cos 2\theta + 4y + 3z = 0$ and $2x + 7y + 7z = 0$. If this system has a non-trivial solution, then for any integer n , the values of θ are given by

(a) $\left[n + \frac{(-1)^n}{3} \right] \pi$ (b) $\left[n + \frac{(-1)^n}{4} \right] \pi$
 (c) $\left[n + \frac{(-1)^n}{6} \right] \pi$ (d) $\frac{n\pi}{2}$

63. If a matrix A is symmetric as well as skew-symmetric, then

(a) A is a diagonal matrix (b) A is a null matrix
 (c) A is a unit matrix (d) A is a triangular matrix

64. If $A = \begin{bmatrix} 3 & 4 \\ 4 & 4 \end{bmatrix}$, and $B = \begin{bmatrix} -2 & -2 \\ 0 & -2 \end{bmatrix}$, then $(A + B)^{-1}$ is

(a) is a skew-symmetric matrix
 (b) $A^{-1} + B^{-1}$
 (c) does not exist
 (d) none of these

65. Let p be an odd prime number and T_p be the following set of matrices

$$T_p = \left\{ A = \begin{bmatrix} a & b \\ c & a \end{bmatrix} : a, b, c \in \{0, 1, 2, \dots, p-1\} \right\}$$

The number of A in T_p such that the trace of A is not divisible by p but $\det(A)$ is divisible by p is

(a) $(p-1)(p^2 - p + 1)$ (b) $p^3 - (p-1)^2$
 (c) $(p-1)^2$ (d) $(p-1)(p^2 - 2)$

EXERCISE SET 2

1. A and B are two non-zero square matrices such that $AB = 0$. Then,

 - both A and B are singular
 - either of them is singular
 - neither matrix is singular
 - none of these

2. If $A \begin{bmatrix} 2 & 3 \\ 4 & 5 \end{bmatrix} = \begin{bmatrix} 0 & -4 \\ 10 & 3 \end{bmatrix}$, then A equals

$\begin{pmatrix} -11 & 4 \\ 2 & -19 \\ -19 & 12 \end{pmatrix}$ (a) $\begin{pmatrix} -11 & 4 \\ 2 & -19 \\ -19 & 12 \end{pmatrix}$	$\begin{pmatrix} -11 & 11 \\ 2 & 2 \\ -19 & -12 \end{pmatrix}$ (b) $\begin{pmatrix} -11 & 11 \\ 2 & 2 \\ -19 & -12 \end{pmatrix}$
$\begin{pmatrix} -8 & 4 \\ -19 & 12 \end{pmatrix}$ (c) $\begin{pmatrix} -8 & 4 \\ -19 & 12 \end{pmatrix}$	$\begin{pmatrix} -16 & 8 \\ -38 & 24 \end{pmatrix}$ (d) $\begin{pmatrix} -16 & 8 \\ -38 & 24 \end{pmatrix}$

3. If A is an n -rowed non-singular square matrix, then $|\text{adj } A|$ is equal to

 - $|A|^n$
 - $|A|^{n-1}$
 - $|A|^{n-2}$
 - $|A|$

4. The inverse of the matrix $A = \begin{bmatrix} 1 & 3 & 3 \\ 1 & 4 & 3 \\ 1 & 3 & 4 \end{bmatrix}$ is equal to

 - $\text{adj } A$
 - $2 \text{ adj } A$
 - A
 - A^T

5. The values of x for which the matrix

$$A = \begin{bmatrix} 3-x & 2 & 2 \\ 2 & 4-x & 1 \\ -2 & -4 & -1-x \end{bmatrix}$$

is singular are

 - 0, 3
 - 1, 3
 - 2, 3
 - 3, 3

6. If $A = \begin{bmatrix} 1 & \log_b a \\ \log_a b & 1 \end{bmatrix}$, then $|A|$ is equal to

 - 1
 - 0
 - $\log_a b$
 - $\log_b a$

7. If A is an invertible matrix, then $\det(A^{-1})$ is equal to

 - 1
 - $|A|$
 - $1/|A|$
 - none of these

26. $A = \begin{bmatrix} 0 & 3 \\ 2 & 0 \end{bmatrix}$ and $A^{-1} = \lambda(\text{adj } A)$, then λ is equal to

- (a) $-\frac{1}{6}$ (b) $\frac{1}{3}$
 (c) $-\frac{1}{3}$ (d) $\frac{1}{6}$

27. If A and B are two matrices such that $A + B$ and AB are both defined, then

- (a) A and B can be any matrices
 (b) A and B are square matrices not necessarily of same order
 (c) A and B are square matrices of same order
 (d) number of columns of A = number of rows of B

28. If $\begin{bmatrix} \cos^2 \theta & \cos \theta \sin \theta \\ \cos \theta \sin \theta & \sin^2 \theta \end{bmatrix} \begin{bmatrix} \cos^2 \phi & \cos \phi \sin \phi \\ \cos \phi \sin \phi & \sin^2 \phi \end{bmatrix}$ is a zero matrix, then θ and ϕ differ by an even multiple of $\pi/2$ (b) odd multiple of $\pi/2$
 (c) even multiple of π (d) odd multiple of π

29. If $A = \begin{bmatrix} i & 0 \\ 0 & i \end{bmatrix}$, then A^{4n} ($n \in N$) equals

- (a) $\begin{bmatrix} 0 & i \\ i & 0 \end{bmatrix}$ (b) $\begin{bmatrix} i & 0 \\ 0 & i \end{bmatrix}$
 (c) $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ (d) $\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$

30. A is a matrix such that $A^2 = 2A - I$, where I is the identity matrix. Then, for $n \geq 2$, A^n is equal to

- (a) $nA - (n-1)I$ (b) $nA - I$
 (c) $2^{n-1}A - (n-1)I$ (d) $2^{n-1}A - I$

31. If A and B are any 2×2 matrices, then $|A+B|=0$ implies

- (a) $|A|+|B|=0$ (b) $|A|=0$ or $|B|=0$
 (c) $|A|=0$ and $|B|=0$ (d) none of these

32. If A and P are 3×3 matrices with integral entries such that $P^TAP = A$, then $\det P$ is

- (a) -1 (b) 1
 (c) ± 1 (d) ± 1 provided A is non-singular

$$\begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & \lambda \end{bmatrix}$$

33. If the matrix $A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & \lambda \end{bmatrix}$ is singular, then λ is

- equal to
 (a) 3 (b) 4
 (c) 2 (d) 5

34. If $1, \omega, \omega^2$ are the cube roots of unity, then

$$\Delta = \begin{vmatrix} 1 & \omega^n & \omega^{2n} \\ \omega^{2n} & 1 & \omega^n \\ \omega^n & \omega^{2n} & 1 \end{vmatrix}$$

has the value

- (a) 0 (b) ω
 (c) ω^2 (d) 1

35. If each element of a 3×3 matrix A is multiplied by 3, then the determinant of the newly formed matrix is

- (a) $3 \det A$ (b) $9 \det A$
 (c) $(\det A)^3$ (d) $27 \det A$

36. The inverse matrix of $\begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & 1 & 1 \end{bmatrix}$ is

- (a) $\begin{bmatrix} \frac{1}{2} & -\frac{1}{2} & \frac{1}{2} \\ -4 & 3 & -1 \\ \frac{5}{2} & -\frac{3}{2} & \frac{1}{2} \end{bmatrix}$ (b) $\begin{bmatrix} \frac{1}{2} & -4 & \frac{5}{2} \\ 1 & -6 & 3 \\ 1 & 2 & -1 \end{bmatrix}$
 (c) $\frac{1}{2} \begin{bmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \\ 4 & 2 & 3 \end{bmatrix}$ (d) $\frac{1}{2} \begin{bmatrix} 1 & -1 & -1 \\ -8 & 6 & -2 \\ 5 & -3 & 1 \end{bmatrix}$

37. If A is a 3×3 non-singular matrix, then $\det [\text{adj } A]$ is equal to

- (a) $(\det A)^2$ (b) $(\det A)^3$
 (c) $\det A$ (d) $(\det A)^{-1}$

38. The inverse of the matrix $\begin{bmatrix} \cos 2\theta & -\sin 2\theta \\ \sin 2\theta & \cos 2\theta \end{bmatrix}$ is

- (a) $\begin{bmatrix} \cos 2\theta & -\sin 2\theta \\ \sin 2\theta & \cos 2\theta \end{bmatrix}$ (b) $\begin{bmatrix} \cos 2\theta & \sin 2\theta \\ \sin 2\theta & -\cos 2\theta \end{bmatrix}$
 (c) $\begin{bmatrix} \cos 2\theta & \sin 2\theta \\ \sin 2\theta & \cos 2\theta \end{bmatrix}$ (d) $\begin{bmatrix} \cos 2\theta & \sin 2\theta \\ -\sin 2\theta & \cos 2\theta \end{bmatrix}$

39. If α, β and γ are the roots of the equation

$x^3 + px + q = 0$, then the value of $\det \begin{bmatrix} \alpha & \beta & \gamma \\ \beta & \gamma & \alpha \\ \gamma & \alpha & \beta \end{bmatrix}$ is

- (a) p (b) q
 (c) $p^2 - 2q$ (d) 0

40. Let $F(\alpha) = \begin{bmatrix} \cos \alpha & -\sin \alpha & 0 \\ \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix}$, then $[F(\alpha)]^{-1}$ is equal to

- (a) $F(-\alpha)$ (b) $F(\alpha^{-1})$
 (c) $F(2\alpha)$ (d) none of these

Assertion-Reason Type Questions

Each of these questions contains two statements: Statement 1 (Assertion) and Statement 2 (Reason). Each of these questions also has four alternative choices, only one of which is the correct answer. You have to select one of the codes (a), (b), (c), or (d) given below:

- (a) Statement 1 is true, Statement 2 is true; Statement 2 is a correct explanation for Statement 1
 - (b) Statement 1 is true, Statement 2 is true; Statement 2 is not a correct explanation for Statement 1
 - (c) Statement 1 is true; Statement 2 is false
 - (d) Statement 1 is false; Statement 2 is true

- 42. Statement 1:** The matrix $A = \frac{1}{3} \begin{bmatrix} 1 & -2 & 2 \\ -2 & 1 & 2 \\ -2 & -2 & -1 \end{bmatrix}$ is an orthogonal matrix.

orthogonal matrix.

Statement 2: If A and B are orthogonal, then AB is also orthogonal.

- 43. Statement 1:** If A is a skew-symmetric matrix of order 3×3 , then $\det(A) = 0$ or $|A| = 0$.

Statement 2: If A is a square matrix, then $\det(A) = \det(A^T) = \det(-A^T)$.

- 44. Statement 1:** The inverse of $A = \begin{bmatrix} 3 & 4 \\ 3 & 5 \end{bmatrix}$ does not exist.

Statement 2: The matrix A is non-singular.

- 45. Statement 1:** If a matrix of order 2×2 commutes with every matrix of order 2×2 , then it is a scalar matrix.

Statement 2: A scalar matrix of order 2×2 commutes with every 2×2 matrix.

46. Statement 1: $\begin{bmatrix} 3 & 0 & 0 \\ 0 & 4 & 0 \\ 0 & 0 & 7 \end{bmatrix}$ is a diagonal matrix.

Statement 2: If $A = [a_{ij}]$ is a square matrix such that $a_{ij} = 0, \forall i \neq j$, then A is called a diagonal matrix.

Previous Years' Questions

47. If $a > 0$ and discriminant of $ax^2 + 2bx + c < 0$ is greater

than zero, then $\begin{vmatrix} a & b & ax+b \\ b & c & bx+c \\ ax+b & bx+c & 0 \end{vmatrix}$ is

- (a) positive
 - (b) $(ac - b^2)(ax^2 + 2bx + c)$
 - (c) negative
 - (d) 0

- 48.** If l, m, n are the p th, q th, r th terms of a G.P., all positive,

then $\begin{bmatrix} \log l & p & 1 \\ \log m & q & 1 \\ \log n & r & 1 \end{bmatrix}$ equals

49. Let $A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$ and $B = \begin{pmatrix} a & 0 \\ 0 & b \end{pmatrix}$, $a, b \in N$. Then

 - (a) there cannot exist any B such that $AB = BA$
 - (b) there exists more than one but a finite number of B 's such that $AB = BA$
 - (c) there exists exactly one B such that $AB = BA$
 - (d) there exist infinitely many B 's such that $AB = BA$

50. If $A = \begin{bmatrix} a & b \\ b & a \end{bmatrix}$ and $A^2 = \begin{bmatrix} \alpha & \beta \\ \beta & \alpha \end{bmatrix}$, then

- (a) $\alpha = 2ab, \beta = a^2 + b^2$
 (b) $\alpha = a^2 + b^2, \beta = ab$
 (c) $\alpha = a^2 + b^2, \beta = 2ab$
 (d) $\alpha = a^2 = b^2, \beta = a^2 - b^2$

51. If the system of equations $x + 2ay + az = 0$, $x + 3by + bz = 0$ and $x + 4cz + cz = 0$ has a non-zero solution, then a, b, c

 - are in G.P.
 - are in H.P.
 - satisfy $a + 2b + 3c = 0$
 - are in A.P.

52. If $\begin{vmatrix} a & a^2 & 1+a^3 \\ b & b^2 & 1+b^3 \\ c & c^2 & 1+c^3 \end{vmatrix} = 0$ and vectors $(1,a,a^2), (1,b,b^2)$ and

- $(1, c, c^2)$ are non-coplanar, then abc equals

53. Let $A = \begin{bmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{bmatrix}$. The only correct statement about

the matrix A is

- (a) A^{-1} does not exist (b) $A = (-1)I$
 (c) A is a zero matrix (d) $A^2 = I$

54. Let $A = \begin{bmatrix} 1 & -1 & 1 \\ 2 & 1 & -3 \\ 1 & 1 & 1 \end{bmatrix}$ and (10) $B = \begin{bmatrix} 4 & 2 & 2 \\ -5 & 0 & \alpha \\ 1 & -2 & 3 \end{bmatrix}$. If B is the inverse of A , then α is
 (a) -2 (b) -1 (c) 2 (d) 5
55. If $A^2 - A + I = 0$, then the inverse of A is
 (a) A (b) $A + I$ (c) $I - A$ (d) $A - I$
56. If $A = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$ and $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$, then which one of the following holds for all $n \geq 1$, by the principle of mathematical induction?
 (a) $A^n = 2^{n-1}A - (n-1)I$ (b) $A^n = nA - (n-1)I$
 (c) $A^n = 2^{n-1}A + (n-1)I$ (d) $A^n = nA + (n-1)I$
57. If $a^2 + b^2 + c^2 = -2$ and

$$f(x) = \begin{vmatrix} 1+a^2x & (1+b^2)x & (1+c^2)x \\ (1+a^2)x & 1+b^2x & (1+c^2)x \\ (1+a^2)x & (1+b^2)x & 1+c^2x \end{vmatrix}$$

 then $f(x)$ is a polynomial of degree
 (a) 0 (b) 1 (c) 2 (d) 3
58. The system of equations

$$\begin{aligned} ax + y + z &= \alpha - 1 \\ x + \alpha y + z &= \alpha - 1 \\ x + y + \alpha z &= \alpha - 1 \end{aligned}$$

 has no solution if α is
 (a) -2 or 1 (b) -2 (c) 1 (d) -1
59. If A and B are square matrices of size $n \times n$ such that $A^2 - B^2 = (A - B)(A + B)$, then which of the following will always be true?
 (a) $A = B$
 (b) $AB = BA$
 (c) either A or B is a zero matrix
 (d) either A or B is an identity matrix
60. If $A = \begin{bmatrix} 5 & 5\alpha & \alpha \\ 0 & \alpha & 5\alpha \\ 0 & 0 & 5 \end{bmatrix}$ and $|A^2| = 25$, then $|\alpha|$ equals
 (a) 1 (b) 1/5 (c) 5 (d) 5^2
61. If $D = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1+x & 1 \\ 1 & 1 & 1+y \end{bmatrix}$ for $x \neq 0, y \neq 0$, then D is
 (a) divisible by x but not by y
 (b) divisible by y but not by x
 (c) divisible by neither x nor y
 (d) divisible by both x and y
62. Let a, b, c be any real numbers. Suppose that there are real numbers x, y, z not all zero such that $x = cy + bz$, $y = az + cx$, $z = bx + ay$, then $a^2 + b^2 + c^2 + 2abc$ equals to
 (a) -1 (b) 1 (c) 0 (d) 2
63. Let A be a square matrix all of whose entries are integers, then which of the following is true?
 (a) If $|A| \neq \pm 1$, then A^{-1} exist, and all its entries are non-integers
 (b) If $|A| = \pm 1$, then A^{-1} exists and all its entries are integers
 (c) If $|A| = \pm 1$, then A^{-1} need not exist
 (d) If $|A| = \pm 1$, then A^{-1} exists but all its entries are not necessarily integers
64. If $A = \begin{bmatrix} \alpha & 0 \\ 1 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 0 \\ 5 & 1 \end{bmatrix}$, then the value of α for which $A^2 = B$ is
 (a) 1 (b) -1 (c) 4 (d) no real values
65. If A is a 3×4 matrix and B is a matrix such that $A^T B$ and $B^T A$ are both defined, then the order of B is
 (a) 3×4 (b) 3×3 (c) 4×4 (d) 4×3
66. If $A = \begin{bmatrix} ab & b^2 \\ -a^2 & -ab \end{bmatrix}$, then A is
 (a) idempotent (b) involuntary
 (c) nilpotent (d) scalar
67. For 2×2 matrices A, B and I , if $A + B = I$ and $2A - 2B = I$, then A equals
 (a) $\begin{bmatrix} 1/4 & 0 \\ 0 & 1/4 \end{bmatrix}$ (b) $\begin{bmatrix} 1/2 & 0 \\ 0 & 1/2 \end{bmatrix}$
 (c) $\begin{bmatrix} 3/4 & 0 \\ 0 & 3/4 \end{bmatrix}$ (d) $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$
68. The value of x for which the matrix product

$$\begin{bmatrix} 2 & 0 & 7 \\ 0 & 1 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} -x & 14x & 7x \\ 0 & 1 & 0 \\ x & -4x & -2x \end{bmatrix}$$

 equals an identity matrix is
 (a) 1/2 (b) 1/3 (c) 1/4 (d) 1/5

69. If A and B are square matrices of the same order and A is non-singular, then for a positive integer n , $(A^{-1}BA)^n$ is equal to
 (a) $A^{-n}B^nA^n$ (b) $A^nB^nA^{-n}$ (c) $A^{-1}B^nA$ (d) $n(A^{-1}BA)$
70. If A is a singular matrix, then $\text{adj } A$ is
 (a) singular (b) non-singular
 (c) symmetric (d) not defined
71. If $\omega \neq 1$ is the complex cube root of unity and matrix $H = \begin{bmatrix} \omega & 0 \\ 0 & \omega \end{bmatrix}$, then H^{70} is equal to
 (a) 0 (b) $-H$ (c) H^2 (d) H
72. If the trivial solution is the only solution of the system of equations $x - ky + z = 0$, $kx + 3y - kz = 0$ and $3x + y - z = 0$, then the set of all values of k is
73. Let $A = \begin{bmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ 3 & 2 & 1 \end{bmatrix}$. If u_1 and u_2 are column matrices such that $Au_1 = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$ and $Au_2 = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$, then $u_1 + u_2$ is equal to
 (a) $\begin{bmatrix} -1 \\ 1 \\ 0 \end{bmatrix}$ (b) $\begin{bmatrix} -1 \\ 1 \\ -1 \end{bmatrix}$ (c) $\begin{bmatrix} -1 \\ -1 \\ 0 \end{bmatrix}$ (d) $\begin{bmatrix} 1 \\ -1 \\ -1 \end{bmatrix}$
74. Let P and Q be 3×3 matrices $P \neq Q$. If $P^3 = Q^3$ and $P^2Q = Q^2P$, then determinant of $(P^2 + Q^2)$ is equal to
 (a) -2 (b) 2 (c) 0 (d) -1

ANSWERS**Exercise Set 1**

- | | | | | | | | | | |
|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| 1. (a) | 2. (b) | 3. (c) | 4. (a) | 5. (a) | 6. (d) | 7. (d) | 8. (c) | 9. (d) | 10. (b) |
| 11. (c) | 12. (a) | 13. (d) | 14. (d) | 15. (b) | 16. (c) | 17. (d) | 18. (a) | 19. (c) | 20. (b) |
| 21. (a) | 22. (d) | 23. (a) | 24. (a) | 25. (b) | 26. (c) | 27. (a) | 28. (a) | 29. (a) | 30. (b) |
| 31. (a) | 32. (a) | 33. (d) | 34. (a) | 35. (a) | 36. (b) | 37. (a) | 38. (b) | 39. (d) | 40. (a) |
| 41. (a) | 42. (b) | 43. (c) | 44. (a) | 45. (a) | 46. (a) | 47. (c) | 48. (a) | 49. (c) | 50. (c) |
| 51. (d) | 52. (b) | 53. (a) | 54. (a) | 55. (c) | 56. (a) | 57. (a) | 58. (d) | 59. (b) | 60. (d) |
| 61. (d) | 62. (c) | 63. (b) | 64. (d) | 65. (c) | | | | | |

Exercise Set 2

- | | | | | | | | | | |
|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| 1. (b) | 2. (c) | 3. (b) | 4. (a) | 5. (a) | 6. (b) | 7. (c) | 8. (d) | 9. (b) | 10. (b) |
| 11. (b) | 12. (d) | 13. (c) | 14. (a) | 15. (d) | 16. (b) | 17. (b) | 18. (b) | 19. (d) | 20. (b) |
| 21. (b) | 22. (b) | 23. (c) | 24. (d) | 25. (b) | 26. (a) | 27. (c) | 28. (b) | 29. (c) | 30. (a) |
| 31. (d) | 32. (d) | 33. (a) | 34. (a) | 35. (d) | 36. (a) | 37. (a) | 38. (d) | 39. (d) | 40. (a) |
| 41. (a) | 42. (b) | 43. (c) | 44. (d) | 45. (a) | 46. (b) | 47. (c) | 48. (d) | 49. (d) | 50. (c) |
| 51. (b) | 52. (a) | 53. (d) | 54. (d) | 55. (c) | 56. (b) | 57. (c) | 58. (b) | 59. (b) | 60. (b) |
| 61. (d) | 62. (b) | 63. (b) | 64. (d) | 65. (a) | 66. (c) | 67. (c) | 68. (d) | 69. (c) | 70. (a) |
| 71. (d) | 72. (a) | 73. (d) | 74. (c) | | | | | | |

To be continued ...

Prepared by -

SANJAY BHATTACHARYA, (Asst. Teacher)

SUKUMAR MANDAL, (Asst. Teacher)

Bibliography

- 1. NCERT MATHEMATICS.**
- 2. SHARMA R.D. , ISC MATHEMATICS , D.R. PUBLICATIONS (P) LTD.**
- 3. DE SOURENDRANATH , MATHEMATICS , CHHAYA PRAKASHANI PVT. LTD.**
- 4. AGGARWAL M.L. , UNDERSTANDING MATHEMATICS , ARYA PUBLICATIONS (P) LTD.**
- 5. AGGARWAL R.S. , SENIOR SECONDARY SCHOOL MATHEMATICS , BHARATI BHAWAN PUBLISHERS.**
- 6. <https://en.wikipedia.org/>**
- 7. <https://www.google.co.in/>**