

ST. LAWRENCE HIGH SCHOOL



A JESUIT CHRISTIAN MINORITY INSTITUTION

CLASS 8

SUBJECT : Algebra and Geometry Work sheet 13 answer key Marks: 15CONGRUENCY AND INEQUALITIES IN TRIANGLES

Date:27.2.21

Answer all the following questions $(1 \times 15 = 15)$

MULTIPLE-CHOICE QUESTIONS (MCQ)

Choose the correct answer in each of the following:

- 1. Which of the following is not a criterion for congruence of triangles?
 - (a) SSA
- (b) SAS
- (c) ASA
- (d) SSS
- 2. If AB = QR, BC = RP and CA = PQ then which of the following holds?
 - (a) $\triangle ABC \cong \triangle PQR$

(b) $\triangle CBA \cong \triangle PQR$

(c) $\triangle CAB \cong \triangle PQR$

(d) $\triangle BCA \cong \triangle PQR$

- 3. If $\triangle ABC \cong \triangle PQR$ then which of the following is not true?

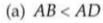
 - (a) BC = PQ (b) AC = PR
- (c) BC = QR
- (d) AB = PQ
- **4.** In $\triangle ABC$, AB = AC and $\angle B = 50^{\circ}$. Then, $\angle A = ?$
- (b) 50°
- (d) 130°
- 5. In $\triangle ABC$, BC = AB and $\angle B = 80^\circ$. Then, $\angle A = ?$
 - (a) 50°
- (b) 40°
- (c) 100°
- (d) 80°
- 6. In $\triangle ABC$, $\angle C = \angle A$, BC = 4 cm and AC = 5 cm. Then, AB = ?
 - (a) 4 cm
- (b) 5 cm
- (c) 8 cm
- (d) 2.5 cm
- 7. Two sides of a triangle are of length 4 cm and 2.5 cm. The length of the third side of the triangle cannot be
 - (a) 6 cm
- (b) 6.5 cm
- (c) 5.5 cm
- (d) 6.3 cm

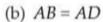
- **8.** In $\triangle ABC$, if $\angle C > \angle B$, then
 - (a) BC > AC
- (b) AB > AC
- (c) AB < AC (d) BC < AC
- 9. It is given that $\triangle ABC \cong \triangle FDE$ in which AB = 5 cm, $\angle B = 40^{\circ}$, $\angle A = 80^{\circ}$ and FD = 5 cm. Then, which of the following is true?
 - (a) $\angle D = 60^{\circ}$
- (b) $\angle E = 60^{\circ}$
- (c) $\angle F = 60^{\circ}$
- (d) $\angle D = 80^{\circ}$
- **10.** In $\triangle ABC$, $\angle A = 40^{\circ}$ and $\angle B = 60^{\circ}$. Then, the longest side of $\triangle ABC$ is
 - (a) BC

(b) AC

(c) AB

- (d) cannot be determined
- 11. In the given figure, AB > AC. Then, which of the following is true?

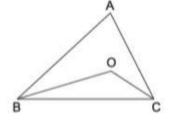




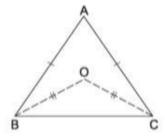
- (c) AB > AD
- (d) Cannot be determined
- **12.** In the given figure, *AB* > *AC*. If *BO* and *CO* are the bisectors of $\angle B$ and $\angle C$ respectively then



- (b) OB > OC
- (c) OB < OC



- **13.** In the given figure, AB = AC and OB = OC. Then, $\angle ABO : \angle ACO = ?$
 - (a) 1:1
 - (b) 2:1
 - (c) 1:2
 - (d) none of these



ANSWERS (MCQ) 1. (a) 2. (c) 3. (a) 4. (c) 5. (a) 6. (a) 7. (b) 8. (b) 9. (b) 10. (c) 11. (c) 12. (b) 13. (a) 14. (b) 15. (b)

- 14. If the altitudes from two vertices of a triangle to the opposite sides are equal then the triangle is
 - (a) equilateral

(b) isosceles

(c) scalene

- (d) right angled
- **15.** In $\triangle ABC$ and $\triangle DEF$, it is given that AB = DE and BC = EF. In order that $\triangle ABC \cong \triangle DEF$, we must have
 - (a) $\angle A = \angle D$
- (b) $\angle B = \angle E$
- (c) $\angle C = \angle F$
- (d) none of these

- 1. SSA is not a criterion for congruence of triangles.
- 2. Clearly, $\downarrow \downarrow \downarrow \downarrow$ Q R P

So, $\triangle CAB \cong \triangle PQR$.

- 3. $\triangle ABC \cong \triangle PQR \Rightarrow BC = QR$.
 - \therefore BC = PQ is not true.
- 4. $AB = AC \implies \angle C = \angle B = 50^{\circ}$. So, $\angle A + 50^{\circ} + 50^{\circ} = 180^{\circ} \implies \angle A = 80^{\circ}$.
- 5. $BC = AB \implies \angle A = \angle C = x^{\circ} \text{ (say)}.$ Then, $x + 80 + x = 180 \implies 2x = 100 \implies x = 50.$
- 6. $\angle C = \angle A \Rightarrow AB = BC = 4$ cm.
- 7. Sum of two sides must be greater than the third side. So, the third side cannot be 6.5 cm.
- 8. $\angle C > \angle B \Rightarrow AB > AC$.
- 9. Given, $\triangle ABC \cong \triangle FDE$.

$$AB = FD = 5 \text{ cm}, \angle B = 40^{\circ} \text{ and } \angle A = 80^{\circ}.$$

$$\angle C = 180^{\circ} - (80^{\circ} + 40^{\circ}) = 60^{\circ}.$$

So, we must have $\angle E = \angle C = 60^{\circ}$.

- 10. $\angle C = 180^{\circ} (40^{\circ} + 60^{\circ}) = 80^{\circ}$. So, the longest side is *AB*.
- 11. $AB > AC \implies \angle ACB > \angle ABC$.

Ext.
$$\angle ADB > \angle ACD \Rightarrow \angle ADB > \angle ACB > \angle ABC$$

 $\Rightarrow \angle ADB > \angle ABD \Rightarrow AB > AD$.

- 12. $AB > AC \Rightarrow \angle C > \angle B \Rightarrow \frac{1}{2} \angle C > \frac{1}{2} \angle B$ $\Rightarrow \angle OCB > \angle OBC \Rightarrow OB > OC.$
- 13. Join OA.

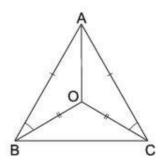
In $\triangle OAB$ and $\triangle OAC$, we have

$$AB = AC$$
 (given),

$$OB = OC$$
 (given)

and OA = OA.

- $\triangle OAB \cong \triangle OAC \Rightarrow \angle ABO = \angle ACO.$
- $\triangle ABO : \angle ACO = 1:1.$



14. A $\triangle ABC$ is given in which $BL \perp AC$ and $CM \perp AB$ such that BL = CM. Then, we have to prove that AB = AC.

In $\triangle ABL$ and $\triangle ACM$, we have:

BL = CM (given),

 $\angle BAL = \angle CAM$ (common),

 $\angle ALB = \angle AMC$ (each 90°)

 $\triangle ABL \cong \triangle ACM$ and hence AB = AC.

 $\triangle ABC$ is isosceles.

15. For congruence, we must have $\angle B = \angle E$.



