



ST. LAWRENCE HIGH SCHOOL
A JESUIT CHRISTIAN MINORITY INSTITUTION



STUDY MATERIAL-10

SUBJECT – STATISTICS

1st term

Chapter: DISPERSION

Class: XI

Topic: Range

Date: 10.08.2020

DISPERSION

PART 1

Definition:

The degree of discrepancy or scatterness of a set of observations from its central value is known as dispersion.

So less be the dispersion better is the central value.

Measures of Dispersion:**➤ Absolute measures:**

1. Range
2. Mean deviation
3. Mean square deviation

➤ Relative measures:

1. Coefficient of mean deviation
2. Coefficient of quartile deviation
3. Coefficient of variation

RANGE

It is the difference of the minimum observation from the maximum observation. It is denoted by R.

For ungrouped grouped data

Observations: $x_1, x_2, \dots, \dots, x_n$

$$R_x = x_{(n)} - x_{(1)}$$

For grouped data

Observations: x_1, x_2, \dots, x_n

Frequency: f_1, f_2, \dots, f_n

$$R_x = x_{(n)} - x_{(1)}$$

Properties:

- Change of base or origin and scale

If $y_i = a + b x_i \forall i = 1(1)n$

Then, $R_y = |b| R_x$

Proof:

Case1: b is positive, ie, $b > 0$

$$y_{(n)} = a + b \cdot x_{(n)} \dots \dots \dots (*)$$

$$y_{(1)} = a + b \cdot x_{(1)} \dots \dots \dots (**)$$

Subtracting (**) from (*), we get

$$R_y = b \cdot R_x$$

Case2: b is negative, ie, $b < 0$

$$y_{(n)} = a + b \cdot x_{(1)} \dots \dots \dots (*)$$

$$y_{(1)} = a + b \cdot x_{(n)} \dots \dots \dots (**)$$

Subtracting (**) from (*), we get

$$R_y = -b.R_x$$

Combining case 1 and case 2, we get

$$R_y = |b| R_x.$$

- If all the observations are equal to a constant, the range becomes equal to zero.

If $x_i = k(\text{constant}) \forall i = 1(1)n$,

Then $R_x = 0$

Proof:

$$\begin{aligned} R_x &= x_{(n)} - x_{(1)} \\ &= k - k = 0 \end{aligned}$$

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